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# Ab initio study of defects in CdMnTe: Electronic structure and related properties

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**Abstract:** Band structure, density of states, total energy and magnetic moment are calculated for ideal and defective supercell CdTe and CdMnTe by ab initio method. The optimization of crystal structure and atom relaxation has been carried out. The band gap, local levels in the band gap and magnetic moments are defined for various defective supercell CdTe and CdMnTe in ferromagnetic and antiferromagnetic states. It has been defined that as Mn atoms, the vacancy, interstitial atom and Frenkel pair in the crystal structure form magnetic moment.

**Keywords:** Semimagnetic Semiconductor, Electron Structure, Defect, Vacancy, Interstitial Atom, Frenkel Pair, Ab Initio, Magnetic Moment, Density of States

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## 1. Introduction

Semimagnetic semiconductors (SMS) are the new class materials, including the properties of both ordinary and magnetic semiconductors. The main qualitative difference between SMS and ordinary semiconductors is the exchange interaction between magnetic ions and band charge carriers, which start to appear only within the external magnetic field [1]. The injection of manganese ions to the crystal lattice of  $A^{II}B^{VI}$  compounds and formation of solid solutions  $A^{II}MnB^{VI}$  lead to increase of band-gap width. Thus it is possible to manage these materials' photosensitivity by Mn ions concentration in SMS. These features cause strengthening of a number of effects, as well as Faraday effect in these materials [2, 3]. On the other hand, there are unusual changes of electron structure of these materials in magnetic field, which allows managing properties of these materials with magnetic field and temperature.

The energy spectrum and wave functions of electrons for arbitrary wave vector as well as Faraday effect for  $Cd_{1-x}Mn_xTe$  thin films were obtained in our previous works [3]. We calculated interband Faraday effect in  $Cd_{1-x}Mn_xTe$  in the framework of two band model with taking into account the exchange interaction in a nonquantizing magnetic field.

$Cd_{1-x}Mn_xTe$  SMS are promising materials for  $\gamma$ - and x-ray detectors, solar cells, optic insulator etc. [4]. To obtain high-sensitive and radiation-resistant materials, as well as creation of devices based on them, it is necessary to know the influence of defects on physical properties of  $Cd_{1-x}Mn_xTe$ . Defects in semiconductors not only influence on electrical and optic properties of these materials, but also display their interesting physical properties.

Ab initio calculations of electron structure and magnetic properties of  $Cd_{1-x}Mn_xTe$  were carried out in some works [5-8]. Unlike these works we carried out first principle calculations based on density functional theory (DFT) by using Atomistix ToolKit (ATK) programme for study of defects on structural and magnetic properties of supercell CdTe and  $Cd_{1-x}Mn_xTe$ . In this work we have theoretically investigated electronic band structure (EBS), density of states (DOS) and magnetic moment (MM) for various ideal and defective supercells CdTe and  $Cd_{1-x}Mn_xTe$ .

## 2. Electronic Structure of Ideal and Defective Supercell CdTe

The first-principle calculations of electronic structure of ideal and defective supercells CdTe based on spin- polarized

DFT are performed in the local spin density approximation with regard to Hubbard-U correction (LSDA+U) on double zeta double polarized (DZDP) basis set using licensed program software ATK [9].

In this section it was given the results of calculations of EBS, DOS and MM of ideal and defective supercell Cd32Te32.

### 2.1. Ideal Supercell Cd32Te32

The electronic structures of ideal supercell Cd32Te32 is calculated. It was defined the band gap of ideal supercell Cd32Te32  $E_g = 1.64\text{eV}$ , the lower level of conductivity band  $E_{c\uparrow} = 0.25\text{eV}$  and the upper level of valence band  $E_{v\downarrow} = -1.39\text{eV}$ . The axes indicate to the spin states. The calculated value of the energy gap corresponds to experimentally measured one. In so doing, we have been able to reproduce the experimental value of the energy gap only if Hubbard\_U corrections were accounted for. It has been taken the value of Hubbard-U parameter for 5p-states of Te,  $U_{Te} = 3.7\text{eV}$  [10]. DOS analysis shows that upper levels of valence band located in the range of  $[-5; 0]\text{eV}$ , mainly comes from 5p-states of Te atoms, and lower levels of conductivity band - from 5s-states of Cd atoms (Fig.1). The total energy of the ideal supercell Cd32Te32 is  $E_t = -68285.96\text{eV}$ .

The Cd atoms in bulk configuration (Fig.1a) is indicated by yellow color, Te atoms by red color.

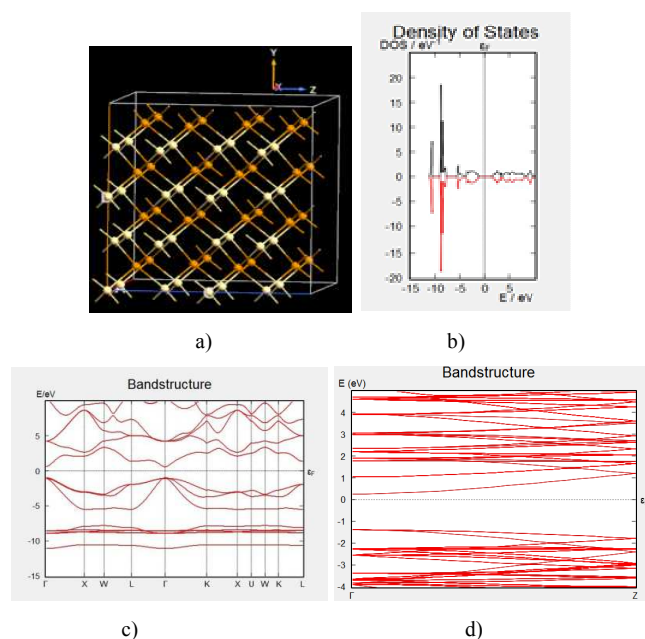


Fig. 1. Ideal supercell Cd32Te32 a) Bulk configuration b) DOS c) EBS for CdTe d) EBS for supercell Cd32Te32

### 2.2. Defective Supercell Cd32Te32

#### 2.2.1. Vacancy in the Supercell Cd32Te32

The Cd vacancy ( $V_{Cd}$ ) in supercell Cd32Te32 leads to rupture of Cd bonds with nearest four Te atoms. The main contribution to the MM give these four anionic atoms with 4 dangling bonds totally  $4.864\mu_B$ , where  $\mu_B$  is the Bohr magneton. The MM of all 32 Te atoms is  $11.276\mu_B$ , and all

31 Cd atoms is  $-9.271\mu_B$ . Finally the total MM of all atoms is  $2.005\mu_B$ . The total amount of electrons is 564, spins of 283 of them directed upward, 281 downward.

Thus, the main contribution to the MM gives 5p orbitals of Te atoms in the upper of the valence band. The contribution from  $p_x$ ,  $p_y$ ,  $p_z$  orbitals are the same. Calculations were performed with an accuracy of  $0.001\mu_B$ .

The electronic structure of supercell Cd32Te32 having  $V_{Cd}$  is calculated (Fig.2). The band gap is changed from  $E_g = 1.64\text{eV}$  to  $E_g = 1.22\text{eV}$ . It is formed no local level in the band gap. The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\downarrow} = 1.47\text{eV}$ ,  $E_{v\uparrow} = 0.25\text{eV}$ . The total energy of the supercell Cd32Te32 with  $V_{Cd}$  is  $E_t = -66730.36\text{eV}$ .

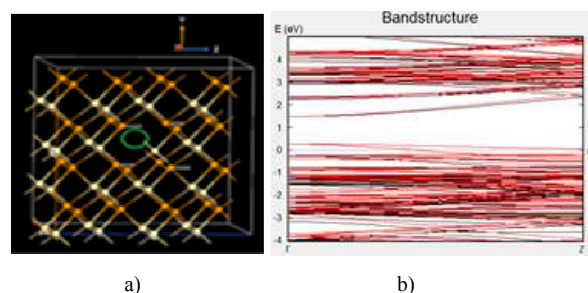


Fig. 2. Supercell Cd32Te32 with  $V_{Cd}$  a) Bulk configuration b) EBS

The contribution to MM of Cd vacancy ( $V_{Cd}$ ) in the supercell Cd32Te32 was defined. 4 anion atoms which have 4 broken bonds near the Cd vacancy, acquires MM  $4.864\mu_B$ . The MM of all 31 Cd atoms is  $-9.271\mu_B$ , and all 32 Te atoms is  $11.276\mu_B$ . The total MM of all atoms is  $2.005\mu_B$ .

The green circle in the Fig.2a indicates to the vacancy site.

The contribution to MM of Te vacancy ( $V_{Te}$ ) in the supercell Cd32Te32 is insignificant. 4 cation atoms which have 4 broken bonds near the Te vacancy, acquires insignificant value of MM  $0.004\mu_B$ . The MM of all 31 Te atoms is  $0.004\mu_B$ , and all 32 Cd atoms is  $0.011\mu_B$ . The total MM of all atoms is  $0.015\mu_B$ .

The band gap is changed from  $E_g = 1.64\text{eV}$  to  $E_g = 1.97\text{eV}$ . It is formed 1 local level in the band gap:  $E_{\uparrow} = 0.21\text{eV}$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\uparrow} = 1.53\text{eV}$ ,  $E_{v\uparrow} = -0.44\text{eV}$  (Fig.3). The total energy of the supercell Cd32Te32 having  $V_{Te}$  is  $E_t = -67692.97\text{eV}$ . The total amount of electrons is 568 and spins of 284 of them directed upward, 284 downward.

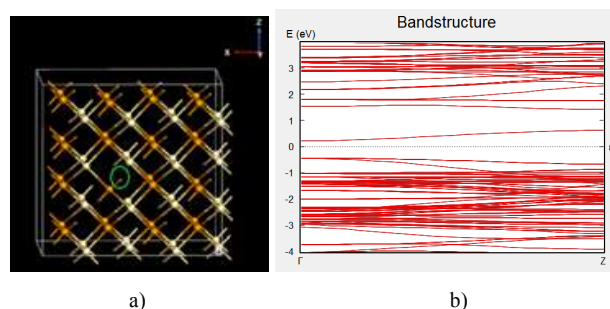


Fig. 3. Supercell Cd32Te32 with  $V_{Te}$  a) Bulk configuration b) EBS

Thus,  $V_{Cd}$  decrease the band gap in the supercell Cd32Te32 but  $V_{Te}$  increase it and forms 1 local level in the band gap.

### 2.2.2. Interstitial Atom in the Supercell Cd32Te32

The electronic structure of supercell Cd32Te32 having interstitial Cd atom ( $I_{Cd}$ ) has been calculated. The band gap doesn't changed. It is formed no local level in the band gap. The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\uparrow}=E_{c\downarrow}=0.58\text{eV}$ ,  $E_{v\uparrow}=E_{v\downarrow}=-1.05\text{eV}$  (Fig.4). The total energy of the supercell Cd32Te32 having  $V_{Cd}$  is  $E_t=-69844.74\text{eV}$ .

$I_{Cd}$  atom has 3 bonds: 2 bonds with Cd atoms and 1 bond with Te atom.  $I_{Cd}$  leads to forming MM. The main contribution to the MM give interstitial Cd atom  $0.489\mu_B$ , two Cd atoms each of them is  $0.399\mu_B$  and Te atom  $1.516\mu_B$  having bonds with interstitial Te atom. The MM of all 33 Cd atoms is  $-1.469\mu_B$  and all 32 Te atoms is  $1.464\mu_B$ . Finally the total MM of all atoms is  $-0.005\mu_B$ .

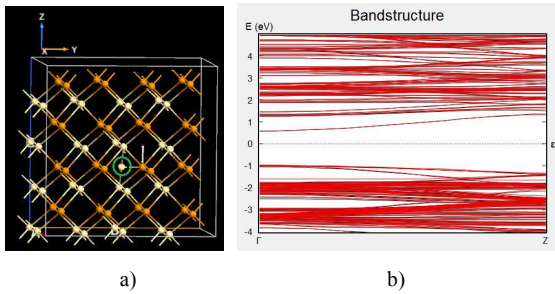


Fig. 4. Supercell Cd32Te32 with  $I_{Cd}$  a) Bulk configuration b) EBS

The electronic structure of supercell Cd32Te32 having interstitial Te atom  $I_{Te}$  has been calculated. The band gap doesn't changed. It is formed 1 local level in the band gap:  $E_{\uparrow}=0.29\text{eV}$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\uparrow}=1.2\text{eV}$ ,  $E_{v\uparrow}=-0.44\text{eV}$  (Fig.5). The total energy of the supercell Cd32Te32 with  $V_{Cd}$  is  $E_t=-68890.2\text{eV}$ .

$I_{Te}$  atom has 5 bonds: 2 bonds with Te atoms and 3 bonds with Cd atoms.  $I_{Te}$  leads to forming large MM. The main contribution to the MM give interstitial Te atom  $5.467\mu_B$ , two Te atoms each of them  $2.521\mu_B$  and 3 Cd atoms each of them  $2.9\mu_B$  having bonds with interstitial Te atom. The MM of all 32 Cd atoms is  $-15.264\mu_B$  and all 33 Te atoms is  $19.891\mu_B$ . Total MM of all atoms is  $4.627\mu_B$ .

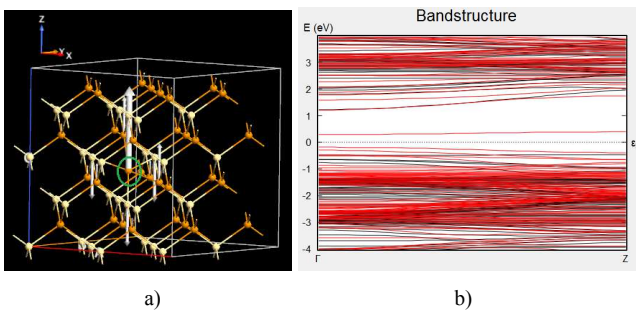


Fig. 5. Supercell Cd32Te32 with  $I_{Te}$  a) Bulk configuration b) EBS

Thus,  $I_{Cd}$  and  $I_{Te}$  atoms in the supercell Cd32Te32 don't change the band gap. It is formed large MM and 1 local level in the band gap in the supercell Cd32Te32 having  $I_{Te}$ .

### 2.2.3. Frenkel Pair in the Supercell Cd32Te32

The displaced Cd atom has 5 bonds with neighboring 2 Cd atoms and 3 Te atoms in the case of Frenkel pair  $F_{Cd}$  in the supercell Cd32Te32.  $F_{Cd}$  in the supercell Cd32Te32 leads to forming 2 local levels in the band gap:  $E_{\uparrow}=0.57\text{eV}$ ,  $E_{\downarrow}=0.43\text{eV}$ . The band gap doesn't changed. The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\downarrow}=1.0\text{eV}$ ,  $E_{v\downarrow\uparrow}=-0.64\text{eV}$  (Fig.6). The total energy of the supercell having  $F_{Te}$  is  $E_t=-68283.4\text{eV}$ .

Frenkel pair  $F_{Cd}$  leads to forming MM. The main contribution to MM give interstitial Cd atom  $-2.36\mu_B$ , two Te atoms each of them  $1.768\mu_B$  and 2 Cd atoms each of them  $0.751\mu_B$  having bonds with interstitial Cd atom and neighboring Te atom  $0.7451\mu_B$ . The MM of all 32 Cd atoms is  $-4.351\mu_B$  and all 32 Te atoms is  $4.35\mu_B$ . Totally MM's of all atoms compensate each other.

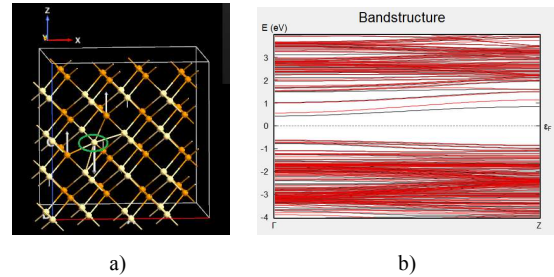


Fig.6. Supercell Cd32Te32 with  $F_{Cd}$  a) Bulk configuration b) EBS

In the case of Frenkel pair  $F_{Te}$  in the supercell Cd32Te32 the displaced Te atom has 5 bonds with neighboring 2 Te atoms and 3 Cd atoms.  $F_{Te}$  in the supercell Cd32Te32 leads to forming 4 local levels in the band gap:  $E_{\uparrow}=-0.05\text{eV}$ ,  $E_{\downarrow}=-0.3\text{eV}$ ,  $E_{\uparrow}=-0.7\text{eV}$ ,  $E_{\downarrow}=-1.0\text{eV}$ . The band gap doesn't changed. The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\uparrow}=0.25\text{eV}$ ,  $E_{v\downarrow\uparrow}=-1.35\text{eV}$  (Fig.7). The total energy of the supercell Cd32Te32 having  $F_{Te}$  is  $E_t=-68286.9\text{eV}$ .

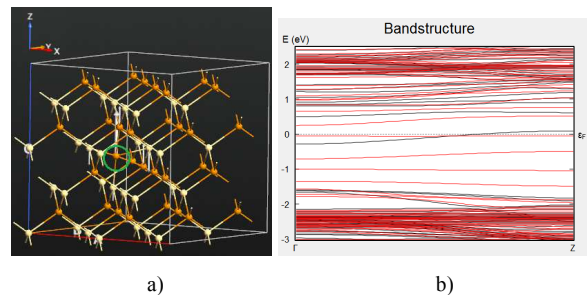


Fig. 7. Supercell Cd32Te32 with  $F_{Te}$  a) Bulk configuration b) EBS

Frenkel pair  $F_{Te}$  leads to forming MM. The main contribution to MM give interstitial Te atom  $3.112\mu_B$ , two Te atoms each of them is  $1.53\mu_B$  and 3 Cd atoms each of them is  $0.751\mu_B$  having bonds with interstitial Cd atom and neighboring Te atom  $1.694\mu_B$ . The MM's of all 32 Cd atoms



is  $-5.35\mu_B$  and all 32 Te atoms is  $6.133\mu_B$ . Finally the total MM of all atoms is  $0.783\mu_B$ .

$F_{Cd}$  and  $F_{Te}$  atoms in the supercell Cd32Te32 don't change the band gap.  $F_{Cd}$  forms 2 local levels and  $F_{Te}$  forms 4 local levels in the band gap in the supercell Cd32Te32. It is formed MM in the supercell Cd32Te32 having  $F_{Cd}$  or  $F_{Te}$  atom.

### 3. Electronic Structure of Defective Supercell $Cd_{1-x}Mn_xTe$

The calculations are performed in ATK program within the spin-polarized DFT and LSDA+U on DZDP basis. We have used  $U_{Mn} = 3.59$  eV for 3d states for Mn atoms and  $U_{Te} = 3.7$  eV for 5p states of Te atoms [10, 11]. It has been given the results of calculations of EBS, DOS and MM of defective supercell Cd30Mn2Te32 in both ferromagnetic and antiferromagnetic states.

#### 3.1. Supercell Cd30Mn2Te32

MM of supercells Cd3MnTe4 and Cd15Mn2Te16 was calculated by ab initio method in the work [13].

We have investigated supercell Cd30Mn2Te32 and have obtained that DOS of supercell Cd30Mn2Te32 consist of three parts in the valence band: 1) the upper part of the valence band is mainly formed from p-states of Te atoms with some contribution of Cd s-states at bottom of the upper part 2) the middle part is formed from d-state of Mn atoms and from s-states of Cd atoms, which are below the valence band maximum on 7eV 3) the main peak at 10 eV below of the valence band maximum is formed mainly from s- states of Te atoms.

The bottom of the conductivity band is formed from s states of Cd atoms and p states of Te atoms. The peak of 2 eV above the conductivity band minimum is formed mainly from d states of Mn atoms [12].

The calculated band gap in ferromagnetic supercell Cd30Mn2Te32 is  $E_g=1.73$ eV, the lower level of conductivity band is  $E_{c\uparrow}=0.632$ eV and the upper level of valence band is  $E_{v\uparrow}=-1.05$ eV (Fig.8). The total energy of the supercell Cd30Mn2Te32 in ferromagnetic supercell Cd30Mn2Te32 is  $E_t=-66403.14$ eV.

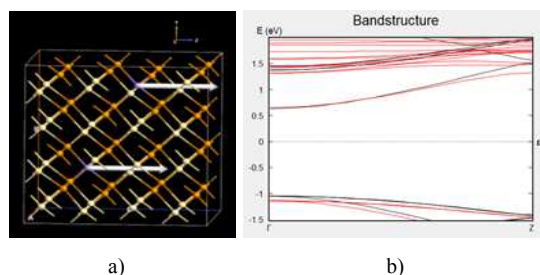


Fig. 8. Supercell Cd30Mn2Te32 in ferromagnetic state a) Bulk configuration b) EBS

For the ferromagnetic supercell Cd30Mn2Te32 the main contribution to the MM give 3d-orbitals of two Mn atoms, the total MM of them is  $10.30\mu_B$ . The MM of all 30 Cd atoms is  $-0.311\mu_B$  and all 32 Te atoms is  $0.406\mu_B$ , they are

practically compensate each other.

The calculated band gap of supercell Cd30Mn2Te32 in antiferromagnetic state is  $E_g=1.73$ eV, the lower level of conductivity band is  $E_{c\downarrow}=0.31$ eV and the upper level of valence band is  $E_{v\downarrow}=-1.42$ eV (Fig.9). The total energy of supercell Cd30Mn2Te32 in antiferromagnetic state is  $E_t=-66403.1$ eV.

For the supercell Cd30Mn2Te32 in antiferromagnetic state the main contribution to the MM give two Mn atoms, each of them leads to formation of MM  $5.113\mu_B$ . The MM of all 30 Cd atoms  $-0.02\mu_B$ , and all 32 Te atoms  $0.024\mu_B$ . The total MM's of all atoms practically compensate each other. The total amount of electrons is 556 and spins of 278 of them directed upward, 278 downward.

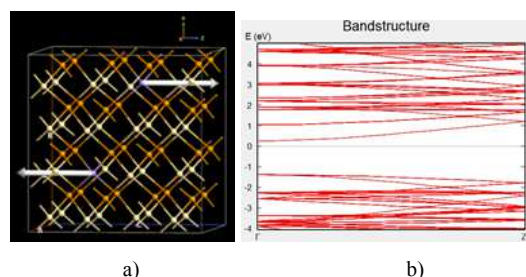


Fig. 9. Supercell Cd30Mn2Te32 in antiferromagnetic state a) Bulk configuration b) EBS

Thus, impurity of two Mn atoms into the supercell Cd30Mn2Te32 leads to forming large MM. Comparison of total energies for ferromagnetic and antiferromagnetic states shows that the antiferromagnetic state is more stable.

#### 3.2. Defective Supercell Cd30Mn2Te32

##### 3.2.1. Vacancy in the Supercell Cd30Mn2Te32

$V_{Cd}$  in the supercell Cd30Mn2Te32 in antiferromagnetic state forms insignificant value of MM. The main contribution to MM give two Mn atoms, each of them leads to formation of MM  $5.321\mu_B$ . The MM which is acquired by four broken Te atoms with dangling bonds near the Cd atom is  $0.319\mu_B$ . The MM of all 29 Cd atoms is  $-0.119\mu_B$  and all 32 Te atoms is  $0.186\mu_B$ . Finally the total MM of all atoms is  $-0.008\mu_B$ .

The band gap doesn't changed  $E_g=1.73$ eV. The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\downarrow}=1.25$ eV,  $E_{v\downarrow}=-0.5$ eV. It is formed 3 local levels in the band gap  $E_{\uparrow}=0$ eV,  $E_{\uparrow}=0.2$ eV,  $E_{\uparrow}=0.6$ eV (Fig.10).

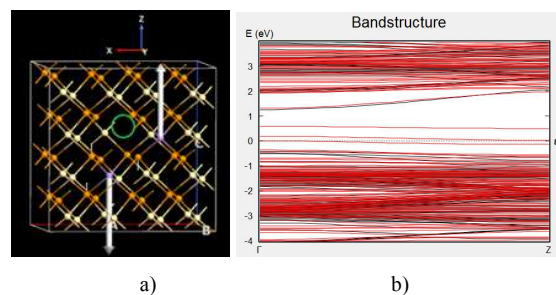


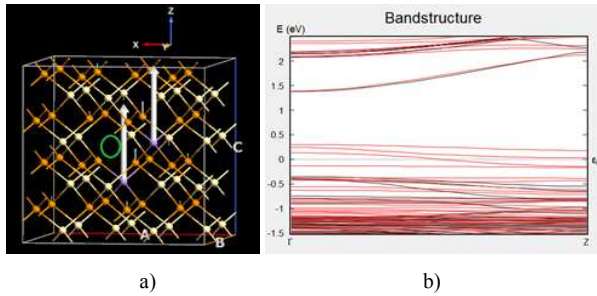
Fig. 10. Supercell Cd30Mn2Te32 with  $V_{Cd}$  in antiferromagnetic state a) Bulk configuration b) EBS

The total energy of supercell Cd30Mn2Te32 having  $V_{Cd}$  in antiferromagnetic state is  $E_t = -64848.24 \text{ eV}$ .

$V_{Cd}$  in the supercell Cd30Mn2Te32 in ferromagnetic state forms large MM due to the two Mn atoms, each of them leads to formation of MM  $5.065 \mu_B$ , and 4 broken Te atoms with dangling bonds near the Cd atom. The MM of all 29 Cd atoms is  $6.309 \mu_B$  and all 32 Te atoms is  $-4.463 \mu_B$ . Finally the total MM of all atoms is  $11.997 \mu_B$ .

The band gap doesn't changed  $E_g = 1.73 \text{ eV}$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\downarrow} = 1.377 \text{ eV}$ ,  $E_{v\downarrow} = -0.35 \text{ eV}$ . It is formed 3 local levels in the band gap  $E_{\uparrow} = 0.3 \text{ eV}$ ,  $E_{\uparrow} = 0.13 \text{ eV}$ ,  $E_{\uparrow} = -0.132 \text{ eV}$  (Fig.11). The total energy of the supercell Cd30Mn2Te32 in ferromagnetic state with  $V_{Cd}$  is  $E_t = -64847.4 \text{ eV}$ .

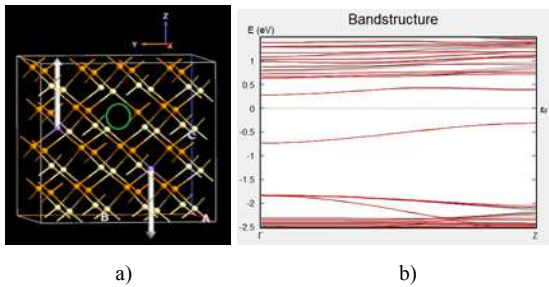
Thus, in the supercell Cd30Mn2Te32 having  $V_{Cd}$  it is formed 3 local levels in the band gap. It is formed MM due to the Mn atoms and Te and Cd vacancies. Comparison of total energies for ferromagnetic and antiferromagnetic states shows that the ferromagnetic state is more stable.



**Fig. 11.** Supercell Cd30Mn2Te32 with  $V_{Cd}$  in ferromagnetic state a) Bulk configuration b) EBS

$V_{Te}$  in the supercell Cd30Mn2Te32 in antiferromagnetic state doesn't form large MM. The main contribution to MM give two Mn atoms, each of them leads to formation of MM  $5.108 \mu_B$ . The MM of all 30 Cd atoms is  $-0.024 \mu_B$  and all 31 Te atoms is  $0.011 \mu_B$ . Finally the total MM of all atoms is  $-0.011 \mu_B$ .

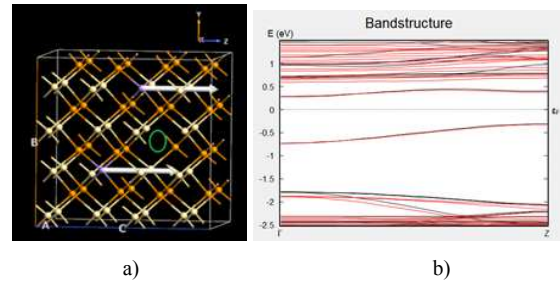
The band gap is changed from  $E_g = 1.73 \text{ eV}$  to  $E_g = 2.1 \text{ eV}$ . It is formed 1 local level in the band gap:  $E_{\uparrow} = -0.731$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\downarrow} = 0.283 \text{ eV}$ ,  $E_{v\downarrow} = -1.83 \text{ eV}$ . The total energy of the supercell Cd30Mn2Te32 in antiferromagnetic state having  $V_{Te}$  is  $E_t = -65817.21 \text{ eV}$  (Fig.12).



**Fig. 12.** Supercell Cd30Mn2Te32 with  $V_{Te}$  in antiferromagnetic state a) Bulk configuration b) EBS

$V_{Te}$  in the supercell Cd30Mn2Te32 in ferromagnetic state doesn't form large MM. The main contribution to MM ferromagnetic supercell Cd30Mn2Te32 give two Mn atoms each of them is  $5.095 \mu_B$ . The MM of all 30 Cd atoms is  $-0.248 \mu_B$  and all 31 Te atoms is  $0.06 \mu_B$ . The total MM of all atoms is  $10.002 \mu_B$ .

The band gap is changed from  $E_g = 1.73 \text{ eV}$  to  $E_g = 2.08 \text{ eV}$ . It is formed 1 local level in the band gap below the Fermi level  $E_{\uparrow\downarrow} = -0.73 \text{ eV}$ . The top of valence band and the bottom of conductivity band are displaced to the energy levels  $E_{c\downarrow} = 0.3 \text{ eV}$ ,  $E_{v\downarrow} = -1.78 \text{ eV}$  (Fig.13). The total energy of the supercell Cd30Mn2Te32 in ferromagnetic state having  $V_{Te}$  is  $E_t = -65817.15 \text{ eV}$ .

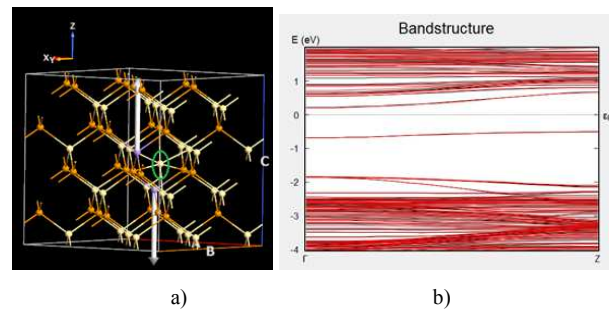


**Fig. 13.** Supercell Cd30Mn2Te32 with  $V_{Te}$  in ferromagnetic state a) Bulk configuration b) EBS

Thus, in the supercell Cd30Mn2Te32 having  $V_{Te}$  it is formed 1 local level in the band gap and band gap is increased. Contribution of  $V_{Te}$  to MM is insignificant. The main contribution to MM gives two Mn atoms. Comparison of total energies for ferromagnetic and antiferromagnetic states shows that the ferromagnetic state is more stable.

### 3.2.2. Interstitial Atom in the Supercell Cd30Mn2Te32

Interstitial Cd ( $I_{Cd}$ ) atom in the supercell Cd30Mn2Te32 in antiferromagnetic state leads to formation of 1 local level in the band gap:  $E_{\uparrow\downarrow} = -0.68 \text{ eV}$ . The band gap is changed from  $E_g = 1.73 \text{ eV}$  to  $E_g = 2.03 \text{ eV}$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\downarrow} = 0.2 \text{ eV}$ ,  $E_{v\downarrow} = -1.83 \text{ eV}$  (Fig.14). The total energy of the supercell Cd30Mn2Te32 in antiferromagnetic state having  $I_{Cd}$  is  $E_t = -67953.46 \text{ eV}$ .



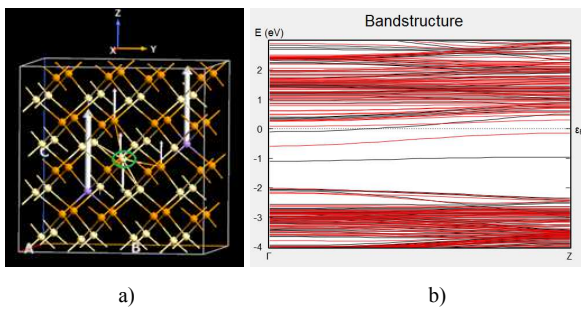
**Fig. 14.** Supercell Cd30Mn2Te32 with  $I_{Cd}$  in antiferromagnetic state a) Bulk configuration b) EBS

Main contribution to the MM give two Mn atoms, each of them is  $5.114 \mu_B$ . The contribution of  $I_{Cd}$  to MM insignificant.

The MM of all 31 Cd atoms is  $-0.023 \mu_B$  and all 32, Te atoms is  $0.079 \mu_B$ . The total MM of all atoms is  $0.006 \mu_B$ .

$I_{Cd}$  atom in the supercell  $Cd_{30}Mn_2Te_{32}$  in ferromagnetic state forms 1 local levels in the band gap:  $E_{\downarrow} = -1.1 \text{ eV}$ . The band gap doesn't changed from. The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{v\uparrow} = -2.31 \text{ eV}$ ,  $E_{c\uparrow} = -0.58 \text{ eV}$  (Fig.15). The total energy of the supercell  $Cd_{30}Mn_2Te_{32}$  in ferromagnetic state having  $I_{Cd}$  is  $E_t = -67953.26 \text{ eV}$ .

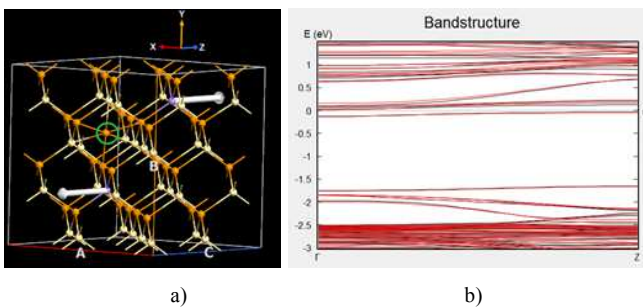
$I_{Cd}$  atom has 6 bonds: 3 bonds with Te atoms and 3 bonds with Cd atoms. The main contribution to the MM give two Mn atoms each of them is  $5.153 \mu_B$ , interstitial Cd atom -  $2.143 \mu_B$  and 3 Te atoms having bonds with interstitial Cd atom, each of them  $2.049 \mu_B$ . The MM of all 31 Cd atoms is  $-4.709 \mu_B$  and all 32 Te atoms is  $4.689 \mu_B$ . The total MM of all atoms is  $10.005 \mu_B$ .



**Fig. 15** Supercell  $Cd_{30}Mn_2Te_{32}$  with  $I_{Cd}$  in ferromagnetic state a) Bulk configuration b) EBS

Thus, in the supercell  $Cd_{30}Mn_2Te_{32}$  having  $I_{Cd}$  it is formed 1 local level in the band gap. Band gap is increased in antiferromagnetic state and doesn't changed in ferromagnetic state. The contribution of  $I_{Cd}$  atom to MM in antiferromagnetic state is insignificant. The main contribution to MM give two Mn atoms and  $I_{Cd}$  atom in ferromagnetic state. Comparison of total energies for ferromagnetic and antiferromagnetic states shows that the ferromagnetic state is more stable.

$I_{Te}$  in the supercell  $Cd_{30}Mn_2Te_{32}$  in antiferromagnetic state it is formed no local level in the band gap. The band gap doesn't changed. The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\uparrow} = 0.1 \text{ eV}$ ,  $E_{v\downarrow} = -1.6 \text{ eV}$ . The total energy of the supercell  $Cd_{30}Mn_2Te_{32}$  in antiferromagnetic state having  $I_{Te}$  is  $E_t = -66981.54 \text{ eV}$  (Fig 16).

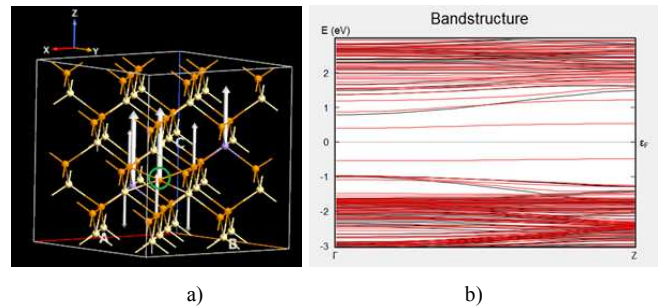


**Fig. 16** Supercell  $Cd_{30}Mn_2Te_{32}$  with  $I_{Te}$  in antiferromagnetic state a) Bulk configuration b) EBS

Main contribution to the MM give two Mn atoms each of them is  $5.64 \mu_B$ .  $I_{Te}$  doesn't lead to formig large MM. The MM of all 30 Cd atoms is  $0.107 \mu_B$  and all 33 Te atoms is  $-0.491 \mu_B$ . The total MM of all atoms is  $-0.006 \mu_B$ .

$I_{Te}$  in the supercell  $Cd_{30}Mn_2Te_{32}$  in ferromagnetic state leads to forming 2 local levels in the band gap:  $E_{\uparrow} = 0.4 \text{ eV}$ ,  $E_{\downarrow} = -0.54 \text{ eV}$ . The band gap doesn't changed  $E_g = 1.73 \text{ eV}$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\downarrow} = 0.783 \text{ eV}$ ,  $E_{v\downarrow} = -0.955 \text{ eV}$  (Fig 17). The total energy of the supercell  $Cd_{30}Mn_2Te_{32}$  in ferromagnetic state with  $I_{Te}$  is  $E_t = -66997.02 \text{ eV}$ .

To move Te atom from its position to the interstitial one it is have to break 4 bonds with Cd atoms. After the displacement the interstitial Te atom has 6 bonds - 3 bonds with Te atoms and 3 bonds with Cd atoms. Contribution to MM give these 6 atoms, each Cd atom  $-2.443 \mu_B$  and each Te atom  $2.823 \mu_B$ , interstitial Te atom itself  $4.632 \mu_B$  and two Mn atoms each of them  $4.806 \mu_B$ . The MM of all 30 Cd atoms is  $-9.16 \mu_B$  and all 33 Te atoms is  $13.52 \mu_B$ . The total MM of all atoms is  $12.994 \mu_B$ .



**Fig. 17** Supercell  $Cd_{30}Mn_2Te_{31}$  with  $I_{Te}$  in ferromagnetic state a) Bulk configuration b) EBS

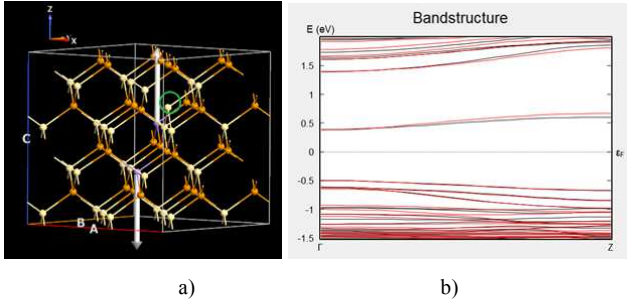
Thus, in the supercell  $Cd_{30}Mn_2Te_{32}$  having  $I_{Te}$  it is formed no local level in the band gap in antiferromagnetic state and 2 local levels in ferromagnetic state. Contribution of  $I_{Te}$  atom to MM in antiferromagnetic state is insignificant. The main contribution to MM give two Mn atoms and  $I_{Te}$  atom in ferromagnetic state. Comparison of total energies for ferromagnetic and antiferromagnetic states shows that the antiferromagnetic state is more stable.

### 3.2.3. Frenkel Pair in the Supercell $Cd_{30}Mn_2Te_{32}$

Frenkel pair  $F_{Cd}$  in the supercell  $Cd_{30}Mn_2Te_{32}$  in antiferromagnetic state leads to forming of 1 local level in the band gap:  $E_{\downarrow} = 0.38 \text{ eV}$ . The band gap is changed from  $E_g = 1.73 \text{ eV}$  to  $E_g = 1.9 \text{ eV}$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\downarrow} = 1.4 \text{ eV}$ ,  $E_{v\downarrow} = -0.5 \text{ eV}$  (Fig.18). The total energy of the supercell  $Cd_{30}Mn_2Te_{32}$  in antiferromagnetic state having  $I_{Te}$  is  $E_t = -66400.55 \text{ eV}$ .

The displaced Cd atom has 3 bonds with neighboring Cd atoms. Frenkel pair  $F_{Cd}$  in the supercell  $Cd_{30}Mn_2Te_{32}$  in antiferromagnetic state leads to forming MM. The main contribution to MM give two Mn atoms each of them is  $5.241 \mu_B$ . The MM of all 30 Cd atoms is  $0.221 \mu_B$  and all 32 Te atoms is  $-0.707 \mu_B$ . The total MM of all atoms is  $-0.619 \mu_B$ .

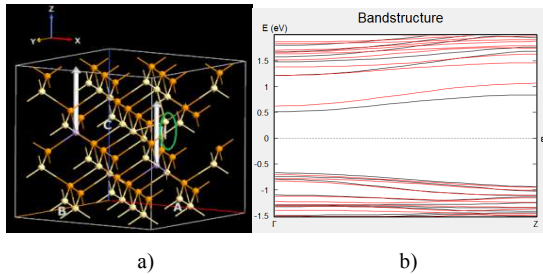




**Fig. 18.** Supercell Cd30Mn2Te31 with  $F_{Cd}$  in antiferromagnetic state a) Bulk configuration b) EBS

Displacement of Cd atom in the supercell Cd30Mn2Te32 in ferromagnetic state leads to forming  $F_{Cd}$ . Cd atom breaks 4 bonds with Te atoms displaces to the interstitial and forms 4 new bonds with 2 Cd atoms and 2 Te atoms.  $F_{Cd}$  in the supercell Cd30Mn2Te32 in ferromagnetic state leads to forming of 2 local levels in the band gap:  $E_{\uparrow}=0.51\text{eV}$ ,  $E_{\downarrow}=0.62\text{eV}$ . The band gap is changed from  $E_g=1.73\text{eV}$  to  $E_g=1.89\text{eV}$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{v\uparrow}=-0.67\text{eV}$ ,  $E_{c\downarrow}=1.215\text{eV}$  (Fig.19). The total energy of the supercell Cd30Mn2Te32 in antiferromagnetic state having  $I_{Te}$  is  $E_t=-66400.88\text{eV}$ .

Frenkel pair  $F_{Cd}$  in ferromagnetic state leads to forming MM. The main contribution to MM give two Mn atoms, each of them  $5.081\mu_B$ , interstitial Cd atom with MM of  $1.372\mu_B$  and two Te atoms with MM of  $1.91\mu_B$  and  $0.3964\mu_B$ . The MM of all 30 Cd atoms is  $-2.663\mu_B$  and all 32 Te atoms is  $2.623\mu_B$ . The total MM of all atoms is  $10.002\mu_B$ .



**Fig. 19.** Supercell Cd30Mn2Te31 with  $F_{Cd}$  in ferromagnetic state a) Bulk configuration b) EBS

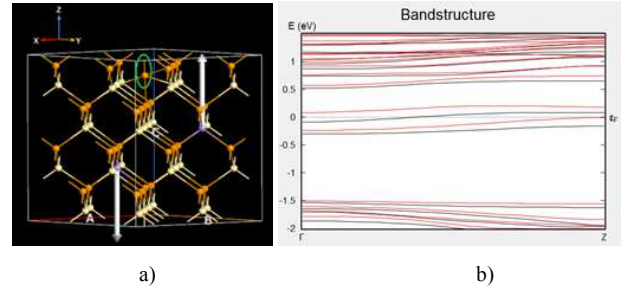
Thus, in the supercell Cd30Mn2Te32 having  $F_{Cd}$  it is formed 1 local level in the band gap in antiferromagnetic state and 2 local levels in ferromagnetic state. The band gap is increased. Contribution of  $F_{Cd}$  atom to MM is insignificant. The main contribution to MM give two Mn atoms. Comparison of total energies for ferromagnetic and antiferromagnetic states shows that the antiferromagnetic state is more stable.

Displacement of Te atom leads to formation of  $F_{Te}$  in the supercell Cd30Mn2Te32. Te atom breaks 4 bonds with Cd atoms displaces to the interstitial position and forms 4 new bonds with 2 Cd atoms and 2 Te atoms.

Frenkel pair  $F_{Te}$  in the supercell Cd30Mn2Te32 in antiferromagnetic state leads to formation of 4 local levels in the band gap:  $E_{\uparrow}=0.8$ ,  $E_{\downarrow}=-0.1\text{eV}$ ,  $E_{\uparrow}=-0.25\text{eV}$ ,  $E_{\downarrow}=-0.3\text{eV}$ .

The band gap is changed from  $E_g=1.73\text{eV}$  to  $E_g=2.0\text{eV}$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{v\downarrow}=-1.5\text{eV}$ ,  $E_{c\downarrow}=0.5\text{eV}$  (Fig.20). The total energy of the supercell Cd30Mn2Te32 in antiferromagnetic state with  $F_{Te}$  is  $E_t=-66398.475\text{eV}$ .

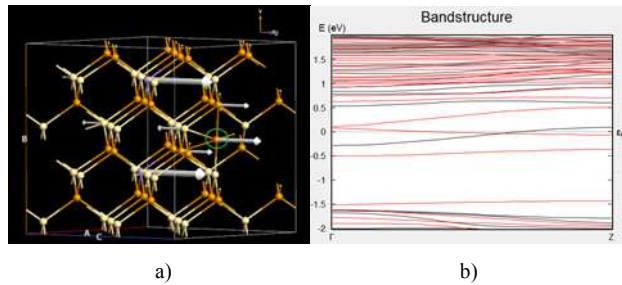
$F_{Te}$  forms insignificant MM. The main contribution to MM gives two Mn atoms each of them  $5.241\mu_B$ . The MM of all 30 Cd atoms is  $-0.221\mu_B$  and all 32 Te atoms is  $0.707\mu_B$ . The total MM of all atoms is  $1.022\mu_B$ .



**Fig. 20.** Supercell Cd30Mn2Te31 with  $F_{Te}$  in antiferromagnetic state a) Bulk configuration b) EBS

Frenkel pair  $F_{Te}$  in the supercell Cd30Mn2Te32 in ferromagnetic state leads to formation of 3 local levels in the band gap:  $E_{\uparrow}=0.1$ ,  $E_{\downarrow}=-0.3\text{eV}$ ,  $E_{\uparrow}=-0.5\text{eV}$ . The band gap is changed from  $E_g=1.73\text{eV}$  to  $E_g=2.0\text{eV}$ . The top of valence band and the bottom of conductivity band are shifted towards the energy levels  $E_{c\uparrow}=0.5\text{eV}$ ,  $E_{v\uparrow}=-1.5\text{eV}$ . The total energy of the supercell Cd30Mn2Te32 in ferromagnetic state having  $I_{Te}$  is  $E_t=-66405.26\text{eV}$ .

Frenkel pair  $F_{Te}$  in the supercell Cd30Mn2Te32 in ferromagnetic state leads to forming MM. The main contribution to MM give two Mn atoms each of them have MM  $5.113\mu_B$  and 4 broken bonds of Cd atoms with Te atom  $-1.717\mu_B$ ,  $-2.175\mu_B$ ,  $-1.667\mu_B$ ,  $-0.919\mu_B$ , and 3 Te atoms  $2.445\mu_B$ ,  $2.423\mu_B$ ,  $3.495\mu_B$ . The MM of all 30 Cd atoms is  $-9.279\mu_B$  and all 32 Te atoms is  $9.9\mu_B$ . The total MM of all atoms is  $10.821\mu_B$ .



**Fig. 21.** Supercell Cd30Mn2Te31 with  $F_{Te}$  in ferromagnetic state a) Bulk configuration b) EBS

Thus, in the supercell Cd30Mn2Te32 having  $F_{Te}$  it is formed 4 local levels in the band gap in antiferromagnetic state and 3 local levels in ferromagnetic state. The band gap is increased. Contribution of  $F_{Te}$  atom to MM in the supercell Cd30Mn2Te32 in antiferromagnetic state is insignificant. The main contribution to MM give two Mn atoms and  $F_{Te}$  in ferromagnetic state. Comparison of total energies for

ferromagnetic and antiferromagnetic states shows that the antiferromagnetic state is more stable.

## 4. Conclusion

It was calculated band structure, density of states and magnetic momentum for ideal and defective supercell CdTe and CdMnTe by ab initio method. The band gap, local levels in the band gap and magnetic momentum are defined for various defects in ferromagnetic and antiferromagnetic states. It has been defined, that as Mn atoms, the vacancy, interstitial atom and Frenkel pair in the crystal structure form magnetic moment.

It has been defined that  $V_{Cd}$  decrease the band gap in the supercell Cd32Te32 but  $V_{Te}$  increase it and forms 1 local level in the band gap.

$I_{Cd}$  and  $I_{Te}$  atoms in the supercell Cd32Te32 don't change the band gap. It is formed large MM and 1 local level in the band gap in the supercell Cd32Te32 having  $I_{Te}$ .

$F_{Cd}$  and  $F_{Te}$  atoms in the supercell Cd32Te32 don't change the band gap.  $F_{Cd}$  forms 2 local levels and  $F_{Te}$  forms 4 local levels in the band gap in the supercell Cd32Te32. It is formed MM in the supercell Cd32Te32 having  $F_{Cd}$  or  $F_{Te}$  atom.

Impurity of two Mn atoms into the supercell Cd30Mn2Te32 leads to forming large MM. The antiferromagnetic phase is more stable in the supercell Cd30Mn2Te32.

In the supercell Cd30Mn2Te32 having  $V_{Cd}$  it is formed 3 local levels in the band gap. It is formed MM due to the Mn atoms, Te and Cd vacancies. The antiferromagnetic state in the supercell Cd30Mn2Te32 having  $V_{Cd}$  is more stable.

In the supercell Cd30Mn2Te32 having  $V_{Te}$  it is formed 1 local level in the band gap and band gap is increased. The contribution of  $V_{Te}$  to MM is insignificant. The main contribution to MM give two Mn atoms. The ferromagnetic state is more stable in the supercell Cd30Mn2Te32 having  $V_{Te}$ .

In the supercell Cd30Mn2Te32 having  $I_{Cd}$  it is formed 1 local level in the band gap. The band gap is increased in antiferromagnetic state and doesn't changed in ferromagnetic state. The contribution of  $I_{Cd}$  atom to MM in antiferromagnetic state is insignificant. The main contribution to MM give two Mn atoms and  $I_{Cd}$  atom in ferromagnetic state. Comparison of total energies for ferromagnetic and antiferromagnetic states shows that the ferromagnetic state is more stable.

In the supercell Cd30Mn2Te32 having  $I_{Te}$  it is formed no local level in the band gap in antiferromagnetic state and 2 local levels in ferromagnetic state. The contribution of  $I_{Te}$  atom to MM in the supercell Cd30Mn2Te32 in antiferromagnetic state having  $I_{Te}$  is insignificant. The main contribution to MM give two Mn atoms and  $I_{Te}$  atom in ferromagnetic state. The antiferromagnetic state is more stable.

In the supercell Cd30Mn2Te32 having  $F_{Cd}$  it is formed 1 local level in the band gap in antiferromagnetic state and 2 local levels in ferromagnetic state. The band gap is increased.

Contribution of  $F_{Cd}$  atom to MM is insignificant. The main contribution to MM give two Mn atoms. The antiferromagnetic state is more stable in the supercell Cd30Mn2Te32 having  $F_{Cd}$ .

In the supercell Cd30Mn2Te32 having  $F_{Te}$  it is formed 4 local levels in the band gap in antiferromagnetic state and 3 local levels in ferromagnetic state. The band gap is increased. Contribution of  $F_{Te}$  atom to MM in the supercell Cd30Mn2Te32 in antiferromagnetic state having  $F_{Te}$  is insignificant. The main contribution to MM give two Mn atoms and  $F_{Te}$  in ferromagnetic state. The antiferromagnetic state is more stable in the supercell Cd30Mn2Te32 having  $F_{Te}$ .

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## References

- [1] P.I. Nikitin, A.I. Savchuk, The Faraday effect in semimagnetic semiconductors, *Sov. Phys. Usp.* v.160, 11, 1990, pp.167-196
- [2] M.A. Mehrabova, I.R. Nuriyev, R.N. Hasanli. Obtaining of perfect  $Cd_{1-x}Mn_xTe$  epitaxial thin films and their use potentials, 5th WSEAS Internat. Conf. on Nanotechnology, Cambridge, UK, February 20-22, p.316-320, 2013
- [3] B.M. Askerov, T.G. Ismailov, M.A. Mehrabova Interband Faraday rotation in semimagnetic semiconductors. *Physica status solidi (b)*, 1991, v.163, pp.k117-k121
- [4] M.A. Mehrabova, H.R. Nuriyev, H.S. Orujov, A.M. Nazarov, R.M. Sadigov, V.N. Poladova. Defect formation energy for charge states and electrophysical properties of CdMnTe, The 7th Internat.Conf. on Photonics, Devices and Systems. Photonics Prague 2014, August 27-29, Czech Republic.
- [5] B. Belgoumène, S. Kouidri, M. Driss Khodja. Pseudopotential calculations for the electronic structure of  $Cd_{1-x}Mn_xTe$ . *Physics Letters A*, Volume 261, Issue 3-4, p. 191-196.
- [6] A.E. Merad, M.B. Kanoun, S. Goumri-Said. Ab initio study of electronic structures and magnetism in ZnMnTe and CdMnTe diluted magnetic semiconductors. *Journal of Magnetism and Magnetic Materials*, Volume 302, Issue 2, 2006, p. 536-542,
- [7] B.J. Min. First-Principles Pseudopotential Total-Energy Calculations of CdTe. *Journal of the Korean Physical Society*, Vol. 30, No. 3, 1997, p. 647\_650
- [8] K.Y.Ko, M.G. Blamire. Temperature-induced magnetic phase transition in bulk Cr-Doped CdTe Crystals. *Journal of the Korean Physical Society*, v.49, №2, 2006, p.591-595
- [9] ATK, <http://quantumwise.com>
- [10] Mehrabova M.A., Nuriyev I. R., Orujov H.S., Electron structure and optical properties of  $Cd_{1-x}Mn_xTe$  thin films. *International Journal of Materials*, 1, 2014, p.63-70
- [11] J.Kaczowski, A.Jezierski. DFT+U Calculations of Transition Metal Doped AIN. *Acta Physica Polonica*, v.116, №5, 2009, p.924-926



- [12] Mehrabova M.A., Orujov H.S., Poladova V.N., First principles calculations for the electronic structure of  $\text{Cd}_{1-x}\text{Mn}_x\text{Te}$  diluted magnetic semiconductors. 8th Internat. Conf.on "Circuits, systems, signal and telecommunications", Tenerife, Spain, January 10-12, 177-182 (2014).
- [13] Shi-Hao Wei, X. G. Gong, Gustavo M. Dalpian, Su- Huai Wei. First-principles study of Mn-induced local magnetic moments in host semiconductors. Physical Review B 71, p.144409-1-6, 2005